

# MAT-080 Section N Problem Set 10

Answers and hints are shown in blue

Name: \_\_\_\_\_

Do not approximate.

1. Evaluate and simplify each expression without using a calculator.

(a)  $16^{3/2} = 64$

(b)  $\sqrt{5}\sqrt{20} = 10$

2. Find the domain of  $h(u) = \sqrt{10u - 3}$ ,  $u \geq \frac{3}{10}$

3. Simplify each expression.

(a)  $\left(\frac{x^{1/2}}{x^{1/3}}\right)^2 = x^{1/3}$

(b)  $\sqrt[3]{24} = 2\sqrt[3]{2}$

(c)  $\sqrt[4]{16x^5y^8} = 2xy^2\sqrt[4]{x}$

(d)  $5^{1/4} \cdot 5^{7/4} = 25$

4. Rationalize the denominator and simplify:  $\frac{2}{\sqrt{16x}} = \frac{\sqrt{x}}{2x}$

5. Rationalize the denominator and simplify:  $\frac{10}{\sqrt{6} - \sqrt{2}} = \frac{5(\sqrt{6} + \sqrt{2})}{2}$

6. For each expression, perform the indicated operation and simplify.

(a)  $5\sqrt{3x} - 3\sqrt{75x} = -10\sqrt{3x}$

(b)  $\sqrt{5}(\sqrt{15x} + 3) = 5\sqrt{3x} + 3$

(c)  $(4 - \sqrt{2x})^2 = 2x - 8\sqrt{2x} + 16$

7. Solve each equation.

(a)  $\sqrt{3x} - 6 = 9 \quad x = 75$

(b)  $\sqrt{x} - x + 6 = 0 \quad x = 9$

8. For each expression, perform the indicated operations and simplify.

(a)  $(2 + 3i) - \sqrt{-25} = 2 - 2i$

(b)  $(2 - 3i)^2 = -5 - 12i$

(c)  $(3 - 2i)(1 + 5i) = 13 + 13i$

9. Write in standard form  $\frac{5 - 2i}{3 + i} = \frac{13}{10} - \frac{11}{10}i$ .

10. Galileo drops from the top of a tower a rock weighing 15 pounds. The speed  $s$  of a falling object is given by the formula  $s = \sqrt{2gh}$ , where  $h$  is the distance in feet the object has fallen.  $g$  is the acceleration due to gravity, about 32 feet per second per second. At the base of the tower the rock hits Aristotle at a speed of 80 feet per second. Estimate the height of the tower.     The tower is about 100 feet tall.